

## Exercise Sheet No 4

May 08, 2002

Deadline: May 15, 2002, before the lecture

**1 bonus point**

**Exercise 4.1** (6 points)

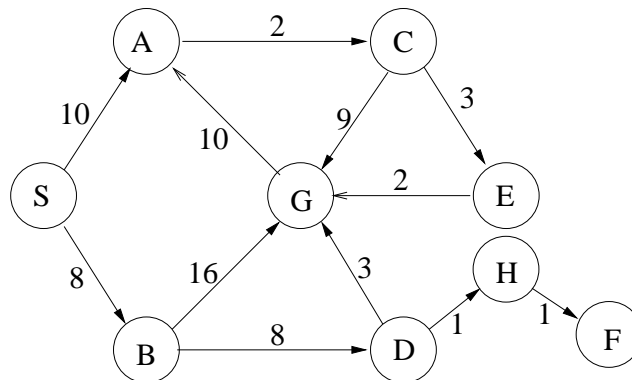
In the lecture, we have noticed that an admissible heuristic (when combined with path-max) leads to monotonically nondecreasing  $f$  values along any path, i.e.  $f(\text{succ}(n)) \geq f(n)$ . Does the implication also hold the other way, i.e. does monotonicity in  $f$  imply admissibility? Prove your answer.

**Exercise 4.2** (7 points)

Perform  $SMA^*$  using

	S	A	B	C	D	E	F	H	G
$h$ -value	12	5	5	5	2	2	1	1	0

as heuristic on the following graph:



Assume that you have enough memory to hold 4 nodes. The node  $S$  is the starting state and  $G$  is the only goal state.

**Exercise 4.3** (7 points)

In this exercise, you will run through the Minimax search strategy on the game *Nim*. The rules of *Nim* are as follows. There are stacks  $s_1, \dots, s_n$  ( $n > 0$ ) of coins in front of two players *Min* and *Max*:



Each stack  $s_i$  consists of  $c_{ij} > 0$  many coins. Each player has a complete and perfect model of the environment and of the possible actions and their effects. The players *Max* and *Min* move alternately, and *Max* moves first. The action a player can perform is to take  $1 \leq l \leq c_{ij}$  many coins away from a single stack  $s_i$ . The player who removes the last (overall) coin wins.

Starting from the initial state (two stacks consisting of 3 and 2 coins), draw the whole game tree. Evaluate the leaf nodes of the tree using the utility function which assigns 1 to win and 0 to loss. Then use Minimax to find the value for the root node. Circle the action that *Max* should take.