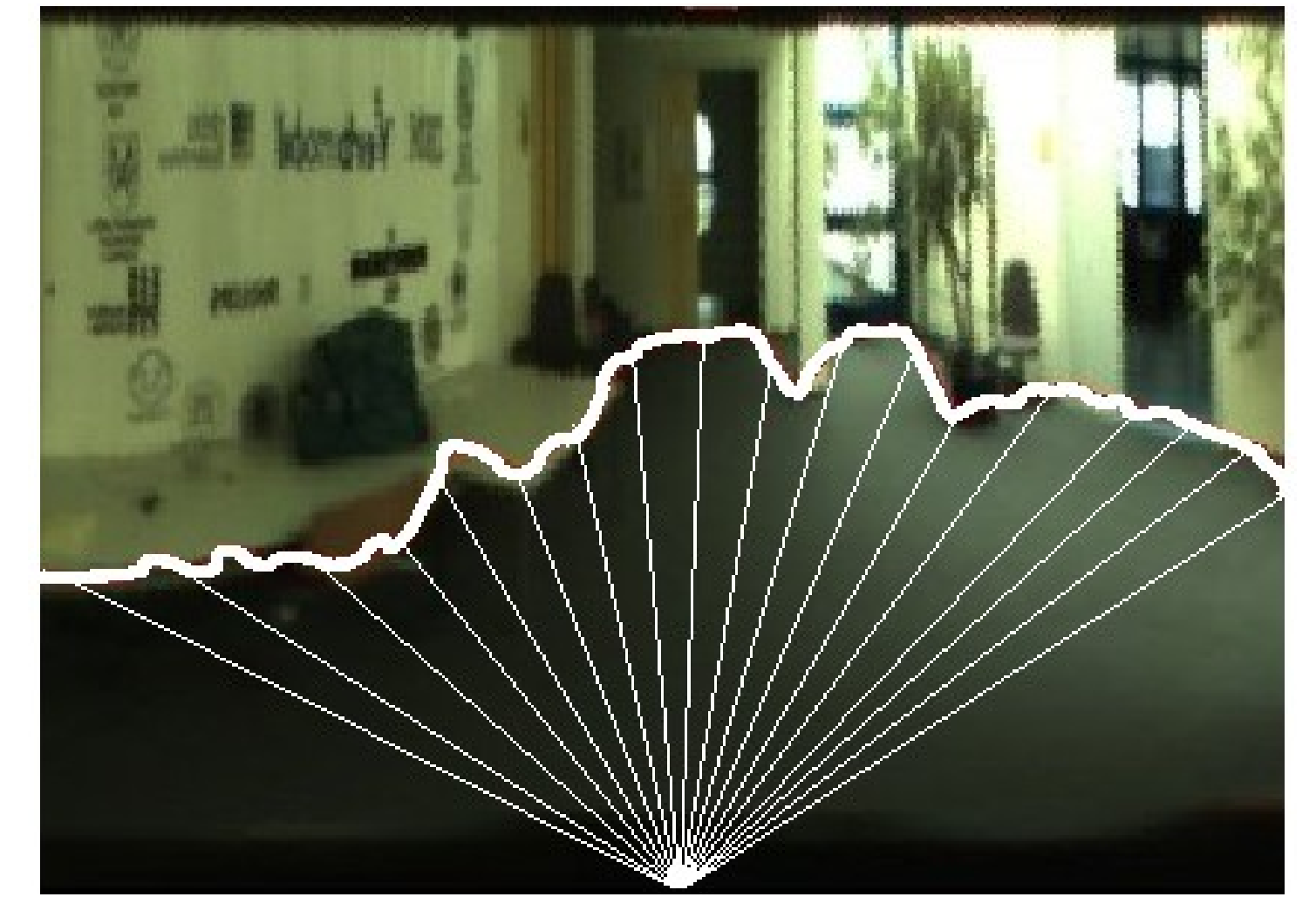


# Monocular Range Sensing: A Non-Parametric Learning Approach

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## Motivation

- Mobile robots need to estimate the geometry of the local surrounding area.
- Cameras are cheap and light-weight sensors but do not measure range directly.
- Idea: Learn the relationship between visual features in monocular camera images and range measurements from a laser sensor.



## Learning Depth from Monocular Camera Images

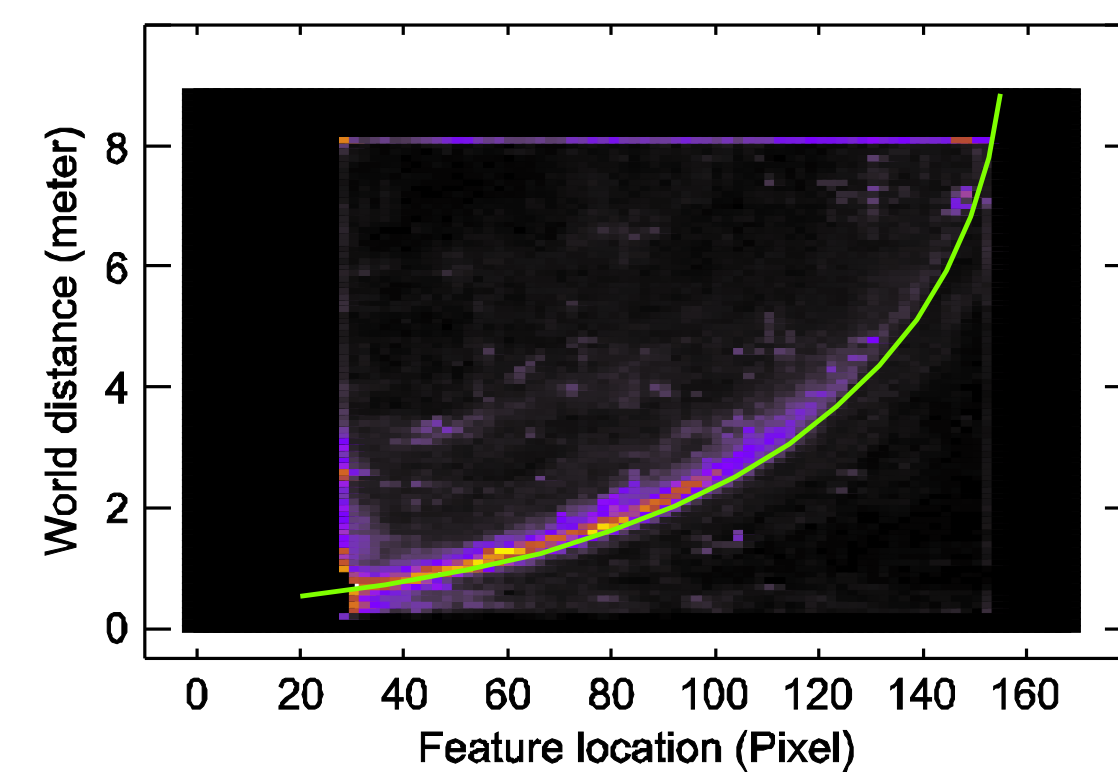
- Training setup: robot + laser + omnidir. camera



- Idea: Learn the range function  $r : \mathbb{R}^{420} \rightarrow \mathbb{R}$  that maps (polar) pixel columns  $\mathbf{P}$  to ranges.

- Pre-processing: Extract features  $\mathbf{x}_i = f(\mathbf{p}_i)$

- Four types of edge-based features
- The first six principle components (PCA)



## Gaussian Process Regression

- Model all ranges as *jointly* Gaussian distributed

$$r_1, \dots, r_n \mid \mathbf{x}_1, \dots, \mathbf{x}_n \sim \mathcal{N}(\boldsymbol{\mu}, \boldsymbol{\Sigma})$$

using a parameterized covariance function, e.g.,

$$k(\mathbf{x}_i, \mathbf{x}_j) = \sigma_f^2 \cdot \exp\left(-\frac{1}{2\ell^2} \|\mathbf{x}_i - \mathbf{x}_j\|^2\right)$$

Then, *new* ranges can be predicted as

$$r^* \mid \mathbf{x}^*, \mathcal{D} \sim \mathcal{N}(\boldsymbol{\mu}^*, \boldsymbol{\sigma}^*)$$

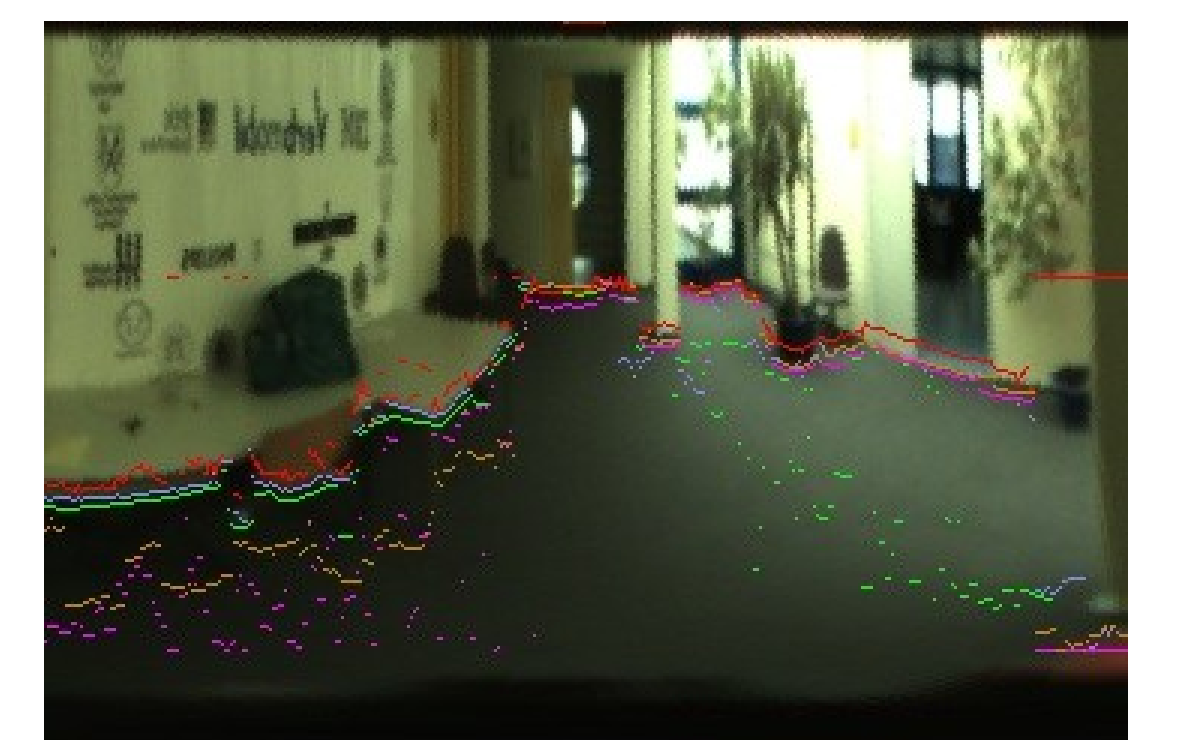
with  $\boldsymbol{\mu}^* = \mathbb{E}[r^*] = \mathbf{k}^{*T} (\mathbf{K} + \sigma_n^2 \mathbf{I})^{-1} \mathbf{r}$

$$\boldsymbol{\sigma}^* = \mathbb{V}[r^*] = \mathbf{k}^{**} - \mathbf{k}^{*T} (\mathbf{K} + \sigma_n^2 \mathbf{I})^{-1} \mathbf{k}^*$$

Covariances  $k(\mathbf{x}^*, \mathbf{x}^*)$   $k(\mathbf{x}^*, \mathbf{x}_i)$   $k(\mathbf{x}_i, \mathbf{x}_i)$

Training targets

- Example of edge-based features (green, pink, blue, brown) and the GP predictions (red)



## Results

- Accuracy of range predictions (RMSE on test set):

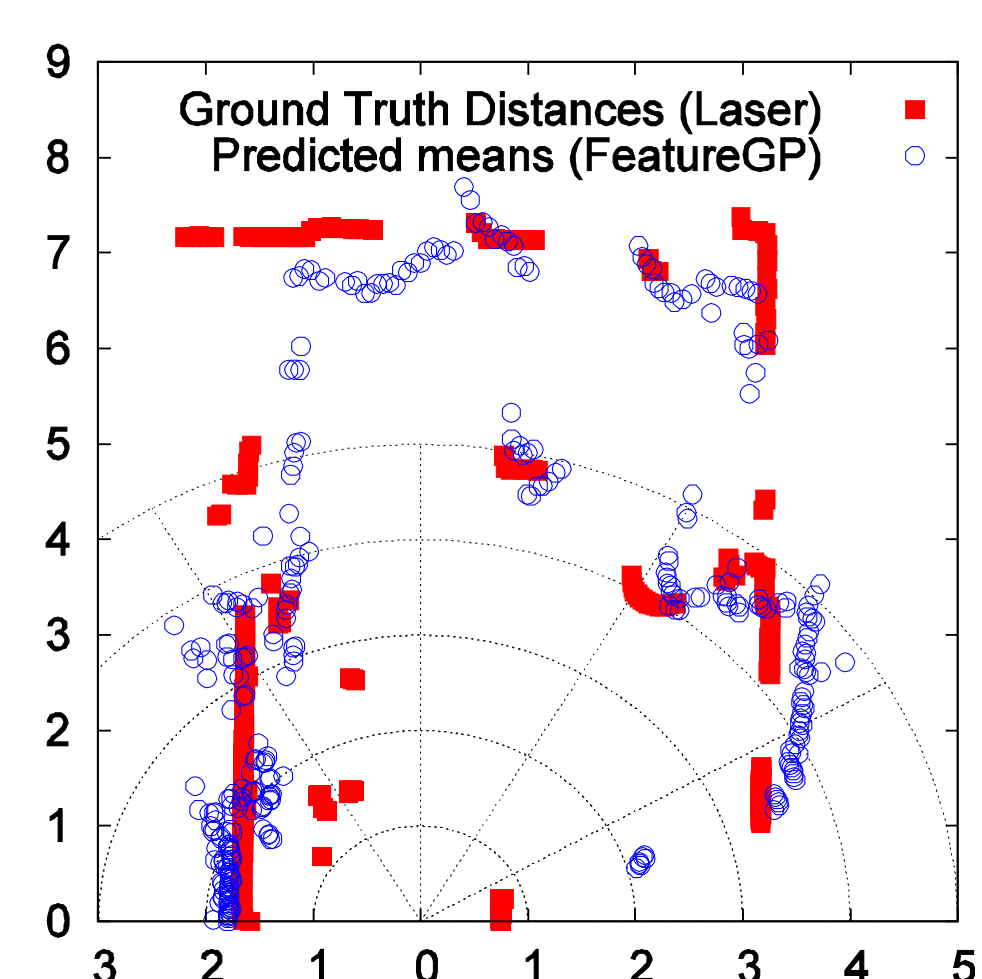
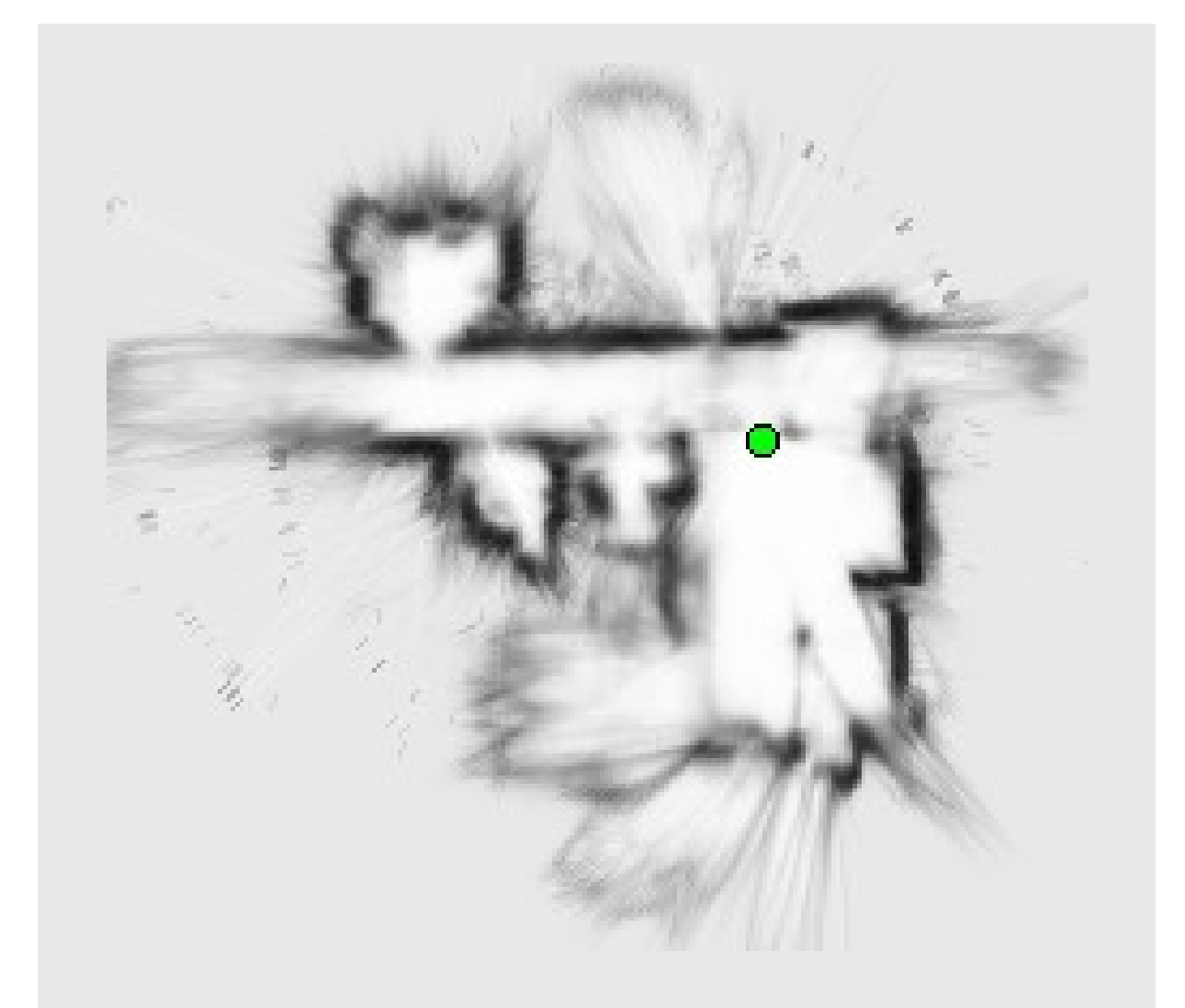
	Saarbrücken	Freiburg
Baseline (Edge-based)	1.70 – 2.06 m	2.08 – 2.87 m
Feature-GP:	1.04 m	1.04 m
Feature-GP + GBP:	1.03 m	0.94 m
LDA-GP + GBP:	1.17 m	1.29 m
PCA-GP + GBP:	1.22 m	1.41 m

- Mapping:

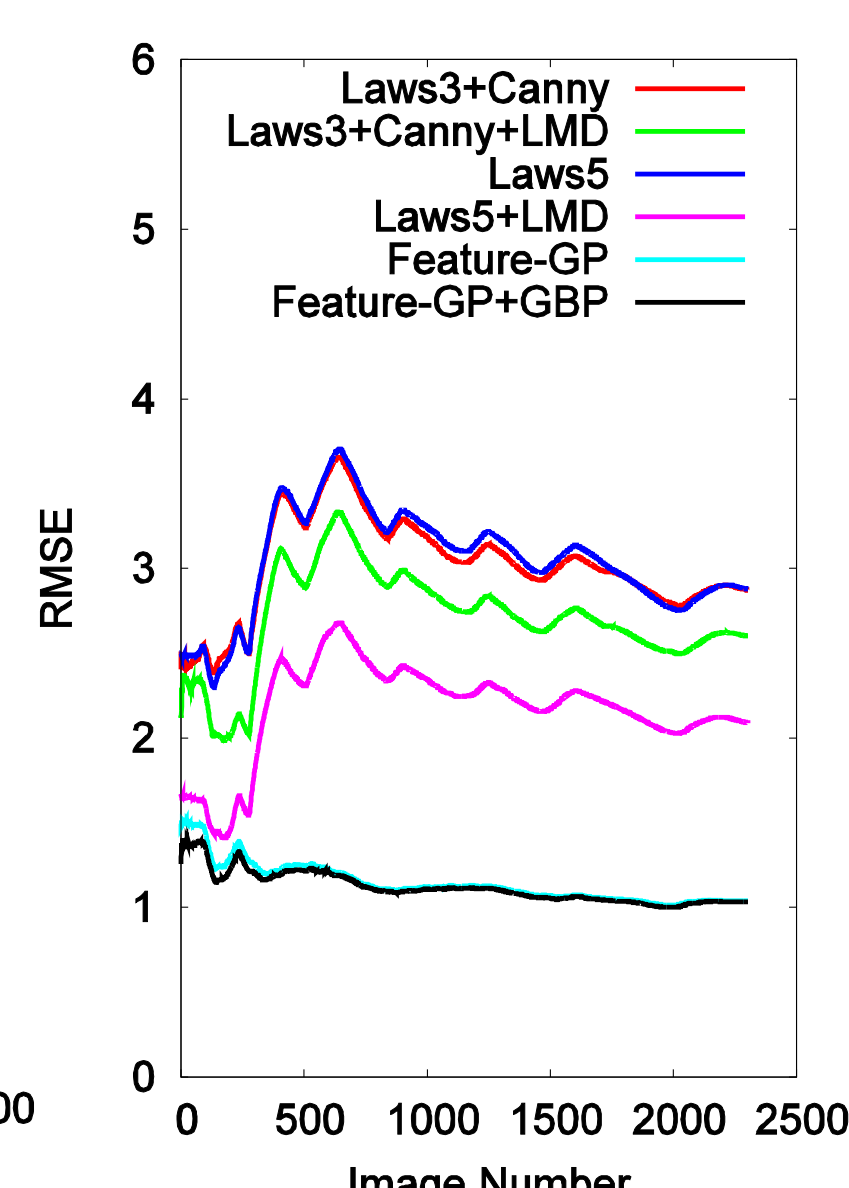
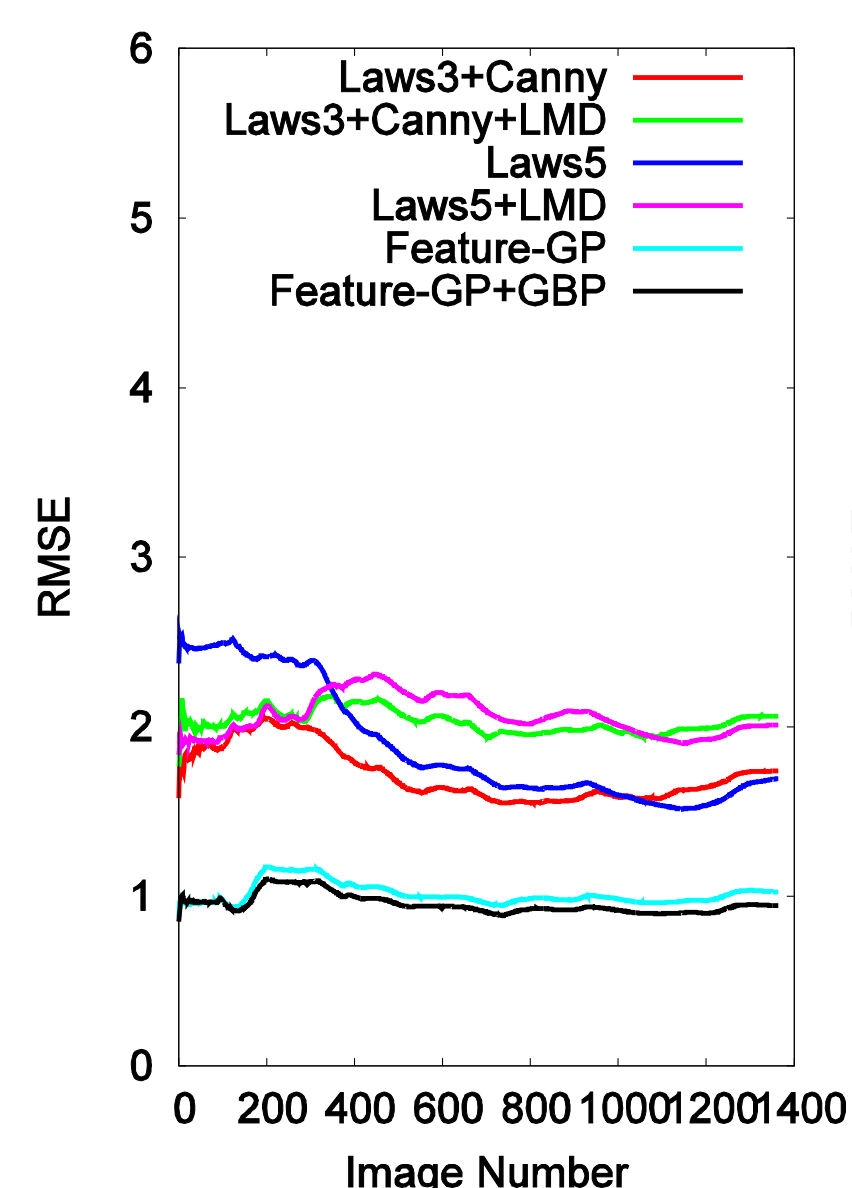
- Predictive uncertainties of the GP can be used in an extended grid mapping algorithm.
- Constructed grid maps using the laser sensor directly vs. the GP predictions.

Laser-based grid map

Feature-GP predictions



Typical 180 degree scan



## Conclusions

- Novel approach for predicting range functions from single, monocular camera images.
- Learning framework: Gaussian process regression utilizing edge-based, LDA and PCA-based visual features.
- Accuracy of range predictions is sufficient, e.g., for local obstacle avoidance (comparable to sonar sensor).